

**Factoring a monomial (GCF) from a polynomial [If factoring is impossible write non-factorable]**

1)  $6a^2 - 15a$

$$3a(2a-5)$$

2)  $32b^2 + 12b$

$$4b(8b+3)$$

3)  $4x^3 - 3x^2$

$$x^2(4x-3)$$

4)  $12a^5b^2 + 16a^4b$

$$4a^4b(3ab+4)$$

5)  $3a^2 - 10b^3$

$$\text{Non-Factorable}$$

6)  $9x^2 + 14y^4$

$$\text{Non-Factorable}$$

7)  $x^5 - x^3 - x$

$$x(x^4 - x^2 - 1)$$

8)  $16x^2 - 12x + 24$

$$4(4x^2 - 3x + 6)$$

9)  $2x^5 + 3x^4 - 4x^2$

$$x^2(2x^3 + 3x^2 - 4)$$

10)  $x^2y^4 - x^2y - 4x^2$

$$x^2(y^4 - y - 4)$$

11)  $x^{2n} + x^n$ , where  $(n > 0)$

$$x^n(x^n + 1)$$

12)  $a^{3n} - a^{2n}$ , where  $(n > 0)$

$$a^{2n}(a^n - 1)$$

13)  $a^{2n+2} + a^2$ , where  $(n > 0)$

$$a^2(a^{2n} + 1)$$

14)  $b^{n+5} - b^5$ , where  $(n > 0)$

$$b^5(b^n - 1)$$

15)  $6t^{2n} - 9t^n$ , where  $(n > 0)$

$$3t^n(2t^n - 3)$$

16)  $12x^2y^2 + 18x^3y - 24x^2y$

$$6x^2y(3x + 2y - 4)$$

17)  $-16a^2b^4 - 4a^2b^2 - 24a^3b^2$

$$-4a^2b^2(6a + 4b^2 + 1)$$

**Factor by Grouping [Note that :  $y - x = -(x - y)$ ]**

18)  $x(a+2)+2(a+2)$

$$(a+2)(x+2)$$

19)  $3(x+y)-a(x+y)$

$$(3-a)(x+y)$$

20)  $a(x-2)-b(2-x)$

$$(x-2)(a+b)$$

21)  $3(a-7)+b(7-a)$

$$(3-b)(a-7)$$

22)  $x^2+3x+2x+6$

$$(x+2)(x+3)$$

23)  $x^2-5x+4x-20$

$$(x-5)(x+4)$$

24)  $xy+4y-2x-8$

$$(x+4)(y-2)$$

25)  $ax+bx-ay-by$

$$(a+b)(x-y)$$

26)  $x^2y-3x^2-2y+6$

$$(x^2-2)(y-3)$$

27)  $2ax^2+bx^2-4ay-2by$

$$(x^2-2y)(2a+b)$$

28)  $x^n y - 5x^n + y - 5$ , where  $(n > 0)$

$$(y-5)(x^n+1)$$

$$(a^n+1)(x^n+2)$$

30)  $x^3+x^2+2x+2$

$$(x+1)(x^2+2)$$

31)  $y^3-y^2+3y-3$

$$(y-1)(y^2+3)$$

32)  $2x^3-x^2+4x-2$

$$(2x-1)(x^2+2)$$

33)  $2y^3-y^2+6y-3$

$$(2y-1)(y^2+3)$$

**Factor Trinomials of the form:  $x^2 + bx + c$ , [If factoring is impossible write non-factorable over the integers.]**

**34)**  $x^2 - 8x + 15$

**35)**  $x^2 + 12x + 20$

**36)**  $a^2 + 12a + 11$

$$\boxed{(x-5)(x-3)}$$

$$\boxed{(x+2)(x+10)}$$

$$\boxed{(a+1)(a+11)}$$

**37)**  $y^2 - 18y + 72$

**38)**  $b^2 + 4b - 32$

**39)**  $b^2 - 6b - 16$

$$\boxed{(y-12)(y-6)}$$

$$\boxed{(b-4)(b+8)}$$

$$\boxed{(b-8)(b+2)}$$

**40)**  $x^2 - 7x - 12$

**41)**  $a^2 - 3ab + 2b^2$

**42)**  $a^2 + 8ab - 33b^2$

$$\boxed{\text{Non-Factorable OTI}}$$

$$\boxed{(a-2b)(a-b)}$$

$$\boxed{(a-3b)(a+11b)}$$

**43)**  $x^2 + 5xy + 6y^2$

$$\boxed{(x+2y)(x+3y)}$$

**Factor Trinomials of the form:  $ax^2 + bx + c$ , where  $a \neq 1$ . [If factoring is impossible write non-factorable over the integers.]**

**44)**  $2x^2 + 7x + 3$

**45)**  $2x^2 - 11x - 40$

**46)**  $4y^2 - 15y + 9$

$$(x+3)(2x+1)$$

$$(x-8)(2x+5)$$

$$(y-3)(4y-3)$$

**47)**  $6b^2 - b - 35$

**48)**  $12y^2 - 13y - 72$

**49)**  $4x^2 + 9x + 10$

$$(2b-5)(3b+7)$$

Non-Factorable OTI

Non-Factorable OTI

**50)**  $6x^2 + 5xy - 21y^2$

**51)**  $4a^2 + 43ab + 63b^2$

**52)**  $18x^2 + 27xy + 10y^2$

$$(2x-3y)(3x+7y)$$

$$(4a+7b)(a+9b)$$

$$(3x+2y)(6x+5y)$$

**53)**  $6 - 7x - 5x^2$

**54)**  $15 - 14a - 8a^2$

**55)**  $35 - 6b - 8b^2$

$$(x+2)(3-5x)$$

$$(2a+5)(3-4a)$$

$$(2b+5)(7-4b)$$

**Using multiple factoring techniques. [If factoring is impossible write non-factorable over the integers.]**

56)  $820x - 8x^2 - 4x^3$

57)  $20x^2 - 38x^3 - 30x^4$

58)  $4x^2y^2 - 32xy + 60$

$$-4x(x^2 + 2x - 205)$$

$$-2x^2(3x+5)(5x-2)$$

$$4(xy-5)(xy-3)$$

59)  $2a^2b^4 + 9ab^3 - 18b^2$

60)  $4x^4 - 45x^2 + 80$

61)  $16x^2y^3 + 36x^2y^2 + 20x^2y$

$$b^2(ab+6)(2ab-3)$$

Non-Factorable OTI

$$4x^2y(y+1)(4y+5)$$

62)  $x^{3n} + 10x^{2n} + 16x^n$

63)  $10x^{2n} + 25x^n - 60$

$$x^n(x^n+2)(x^n+8)$$

$$5(x^n+4)(2x^n-3)$$

**Find all integers  $k$  such that the trinomial can be factored over the integers.**

64)  $x^2 + kx + 8$

65)  $3x^2 + kx + 5$

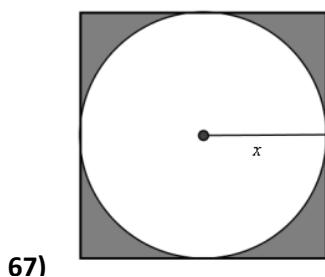
66)  $2x^2 - kx - 5$

$$k = 6, -6, 9, -9$$

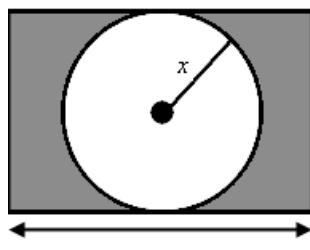
$$k = 8, -8, 16, -16$$

$$k = 3, -3, 9, -9$$

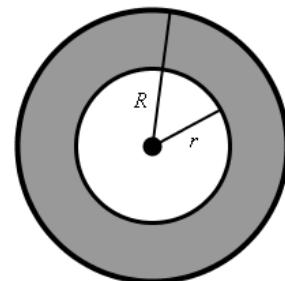
**[Geometry]** Write the area of the shaded region in factored form. Leave your answer in terms of  $\pi$  and the variables shown in the figures below.



67)



68)



69)

$$\text{Area} = x(x - \pi)$$

$$\text{Area} = x^2(10 - \pi)$$

$$\text{Area} = \pi(R^2 - r^2)$$